Molecules Oriented by Brute Force

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The spectroscopy and reaction chemistry of molecules with large dipole moments and small rotational constants that have undergone intense rotational cooling before being introduced into an electric field illustrate that manipulation of the rotational degree of freedom of molecules offers an intriguing challenge.

Techniques to control the orientation of a molecular axis by applying an external field have been sought for many years, because oriented molecules can be used to study the effect on a chemical reaction of the relative orientation of collision partners. The spectroscopy of oriented molecules is also very interesting since free rotational motion is replaced by oscillation over a limited angular range about the field direction (“libration”).

The state-selection and orientation of polar molecules goes back to the celebrated Stern-Gerlach experiment in which a double-peaked diffraction pattern was observed on transmitting a beam of silver atoms through an inhomogeneous magnetic field. Each silver atom exhibited an individual Zeeman effect depending on the angular momentum quantum number, and correlation effects between the silver atoms could be ignored. Orienting a molecule (i.e., aligning preferentially one of the molecule’s ends along a vector fixed in space) means favouring the pointing of its permanent electric dipole moment parallel or antiparallel to an applied electric field. This orientation effect was investigated in the early days of quantum mechanics by measuring the deflection of polar molecules such as HCl in an inhomogeneous electric field. Although strong fields of the order of 4 MV/m were used, the observed deflection was surprisingly small.

This unexpected behaviour can be traced to deviations from the Stern-Gerlach experiment. First, the dipole moment lies along the molecular axis and not, like the magnetic moment, along the angular momentum, so the Stark energy splittings are quadratic in the electric field. Second, in a hot molecular beam, many of the angular momentum quantum rotational sublevels are populated, and each behaves differently.

Subsequent electric deflection experiments investigated the Stark effect of single states, and were not aimed at obtaining an oriented beam. The problem was revived by Paul and coworkers in 1964 who used electric multipolar fields to focus state-selected polar molecules. Kramer and Bernstein [1] pointed out that this method could be used to produce oriented molecular beams of polar symmetric “spinning-top” molecules (e.g., CH3I), and experiments investigating the effect of molecular orientation on reactive scattering followed shortly, although a quantitative interpretation of the observed orientation effects came later [2].

The method of orienting molecules by applying an electric field was known to be inefficient, notably for molecules such as HCl [3]. Reliable methods to produce oriented molecules by simply applying a strong electric field to a molecular beam, which has undergone intense rotational cooling owing to supersonic expansion, had to await the recent pioneering work by Loesch and Remscheid [4] and by Friedrich and Herschbach [5]. As the basic equations have been available for 60 years, the pendular states which arise in these “brute force” experiments are well understood. Many groups are now using brute-force oriented molecules for reaction dynamics, photodissociation and spectroscopic studies.

The Orientation Process

Electric fields in a macroscopic volume rarely exceed 100 MV/m, and values of the order of 10-20 MV/m are typical. Such fields are too weak to modify noticeably the electronic or vibrational structures of most small molecules; but they can strongly modify the rotational motion. For simplicity, consider a linear polar molecule with no net angular momentum other than that due to rotation (i.e., the situation for most molecules in their Σ ground state). The angular momentum J is specified by two quantum numbers, J and M, the latter determining the projection of J on an axis fixed in space; J is perpendicular to the molecular axis. In an electric field, the molecule does not rotate freely owing to the interaction of the dipole D along the molecular axis with the field E.

The Hamiltonian for a rotating dipole in an electric field is \( H = \frac{1}{2} B F - D E \cos \vartheta \), where \( \vartheta \) is the angle between D and E, and B is the rotational constant, which is inversely proportional to the moment of inertia. The eigenstates defined by this Hamiltonian are no longer the free-rotor states \( |J, M\rangle \). The interaction term mixes states \( |J, M\rangle \) with states \( |J, M\rangle \) (M is thus conserved) and when \( D E \) is comparable to, or larger than, the rotational energy splitting \( \Delta E = \hbar B \) to the next higher energy level — strong mixing occurs. The largest effects arise for low-J levels, and the degree of mixing of the parent (or zero-field) state \( |J, M\rangle \) with states \( |J, M\rangle \) is determined by the dimensionless parameter \( \omega = D E / \hbar B \). The table gives the values of the rotational constant B and of the dipole D for a few polar molecules as well as the \( \omega \)-value corresponding to a field E of 10 MV/m.

Since the mixing dampens out progressively with increasing J — J, the energy levels and the associated wavefunctions can easily be calculated by numerical diagonalization of the Hamiltonian matrix on a truncated basis set of free-rotor functions [4, 6]. Many analytical results can also be established using perturbation theory [7]. The eigenfunctions provide the angular distribution function of the dipole rotors.

<table>
<thead>
<tr>
<th>molecule</th>
<th>KCl</th>
<th>KCl</th>
<th>HF (HCN)</th>
</tr>
</thead>
<tbody>
<tr>
<td>D</td>
<td>1.24</td>
<td>10.24</td>
<td>1.874</td>
</tr>
<tr>
<td>B</td>
<td>0.114</td>
<td>0.129</td>
<td>20.96</td>
</tr>
<tr>
<td>( \omega )</td>
<td>18.3</td>
<td>133.3</td>
<td>0.15</td>
</tr>
</tbody>
</table>

Table. Values of the dipole moment D (in Debye) and of the rotational constant B (in cm\(^{-1}\)) for typical molecules. The calculated \( \omega \)-value corresponding to a field E = 10 MV/m is also given.
from which one deduces the average orientation $\langle \cos \theta \rangle$.

Fig. 1 presents the energies of the lowest angular momentum levels as a function of the dimensionless parameter $\omega$. The levels are labelled by $J$ and $M$ of the corresponding zero-field state. At high $\omega$-values the interaction with the field is so strong that the dipoles no longer rotate; in the lowest levels they make only small excursions around the field direction $\mathbf{u} \equiv \hat{u}$, and their motion is well-described by a two-dimensional spherical oscillator.

Consequently, the orientation $\langle \cos \theta \rangle$ of these states is close to 1. Friedrich and Herschbach [5] coined the term "pendular states" to characterise this restrained angular motion of the dipole (these states were also called "librational states" and the motion "hindered rotation").

At small $\omega$-values, each $J$-level (except $J = 0$) is split and molecules in low $M$-levels have a negative orientation. This behaviour is most striking for $M = \omega$, where it is comparable with the classical motion of a hindered rotor. If the dipole has just enough energy to still make full rotations, its angular velocity is considerably larger when $\mathbf{u} = \mathbf{0}$ than when $\mathbf{u} = \hat{u}$. Hence, the dipole resides for a longer time in the antiparallel direction than in the parallel direction and $\langle \cos \theta \rangle < 0$. In a molecular beam, the $M$-averaged rather than the $M$-specific orientation is relevant. For low $\omega$-values, say $\omega < 10^{-2}$, the $M$-averaged orientation is noticeable only for very low $J$-levels ($J < 5$; see Fig. 2). It is therefore very important to produce a rotationally very cold molecular beam ($T_{rot} < 15$ K) in order to obtain an appreciable orientation effect. This is the principle of the brute-force method.

The angular distribution of the dipole averaged over a thermal distribution of parent rotational levels is given approximately by

$$W(\mathbf{u}) = \frac{1 + A_\omega \cos \theta}{2}$$

provided $B \ll kT_{rot}$, and $\omega$ is not too large ($\omega < 10$). The anisotropy parameter $A_\omega = \langle \cos \theta \rangle$ is obtained, in principle, from quantum calculations. Surprisingly, $\langle \cos \theta \rangle$ and thus $A_\omega$ are reproduced to within a few percent by the classical Langevin-Debye relation:

$$\langle \cos \theta \rangle \approx DE/\sqrt[3]{k T_{rot}}$$

Reactive Scattering

Properties of pendular states, in particular the localization near $\mathbf{u} = \mathbf{0}$ of the lowest states, have recently been probed using collisions and spectroscopic measurements. The former employs the brute force technique to investigate steric effects in reactive collisions, i.e., the effect of the orientation of the molecular axis with respect to the relative velocity of the reactants. The first system to be considered [10] was the reaction $K + CH_3l \to KI + CH_3$ which had been studied many years ago using a technique based on hexapole focussing. Subsequently, van Leuken et al. investigated the analogous reaction $K + CH_3Br \to KBr + CH_3$ for which only product angular distributions at thermal energies, but no steric data, were known. The unique feature of the brute-force technique, namely its applicability to all types of polar molecules in $\Sigma$ states, was then exploited in a study of the steric effects involved in the reaction $K + CI \to KCI + I, KI + CI$ [8].

The experimental arrangement common to all three experiments is shown in Fig. 3. Two supersonic beams of seeded reagents intersect at right angles. The products formed in the intersection volume enter a detector chamber were they are ionized on a hot rhenium surface. The detector can be rotated around the intersection volume in the plane containing the two molecular beams in order to measure the angular distributions of products. Product velocity distributions are measured using a standard time-of-flight (TOF) analysis.

Fig. 1. The energies of the lowest $JM$ levels as a function of the dimensionless parameter $\omega$. The levels are labelled $00$, $10$, etc. according to their quantum numbers $JM$ defined at zero field. The energy unit is the rotational constant $B$.

Fig. 2. Plot of the $M$-averaged orientation as a function of $\omega$ for the level $J = 0.5$. Only the lowest $J$-levels contribute significantly to the orientation for modest $\omega$-values. It is thus important to produce a rotationally very cold molecular beam so as to obtain an appreciable orientation effect. This is the principle of the brute-force method.

Fig. 3. A schematic illustration of the crossed molecular-beam apparatus at the University of Bielefeld showing the two molecular beam sources (for K and CI in this case), the rotatable field plates, and the movable detector with the time-of-flight chopper.
Information about product velocities is crucial because both the non-reactively scattered K atoms and the products KX (X denotes a halogen atom) are equally well detected. But, as atoms and products usually travel with drastically different velocities, the TOF distributions can be used to separate out these two contributions to the ion signal.

The orientation field surrounding the intersection volume is generated by two parallel plates which are positioned perpendicular to the plane of the two molecular beams. They each have a slit in this plane to let the beams and the scattered products pass freely. By applying potentials \( \pm U \), a field \( \mathbf{E} \) is generated which can be rotated in the scattering plane by rotating the electrode assembly. Reversion of the field direction is achieved by switching the sign of the potentials.

Assuming a Maxwell-Boltzmann rotational distribution, the distribution of the molecular axis is described by Eq. (1). Quantum calculations provide the following values of the anisotropy parameter \( A_0 \): CH, I (|\( \mathbf{E} \)| = 1.6 MV/m, \( T_{\text{cm}} = 31 \) K): 0.0189; CH, Br (|\( \mathbf{E} \)| = 1.88 MV/m, \( T_{\text{cm}} = 25 \) K): 0.036; ICI (|\( \mathbf{E} \)| = 2.0 MV/m, \( T_{\text{cm}} = 14 \) K): 0.045, where the depolarizing influence of nuclear spins is neglected, in agreement with recent calculations which confirm that the decoupling of nuclear spins and rotational angular momentum is essentially complete for such fields [9].

The relative velocity is well defined because the beam velocity distributions and angular profiles are sufficiently narrow. So cylindrical symmetry of the collision is preserved for the simple case where \( \mathbf{E} \) is parallel or anti-parallel to the relative velocity of the colliding reagents. The flux of products \( f(\Theta, A, B) \) is determined as a function of the laboratory scattering angle \( \Theta_{LAB} \) for the two opposite directions of the field (denoted + and --). One can then define a differential steric effect by:

\[
S(\Theta_{LAB}) = \frac{I_+ (\Theta_{LAB}) - I_- (\Theta_{LAB})}{I_+ (\Theta_{LAB}) + I_- (\Theta_{LAB})}
\]

A similar quantity can also be defined for product fluxes measured as functions of the product velocity in the laboratory frame. The full analysis of the experimental signals is relatively difficult, with much of the complexity coming from the transformation from the collision centre-of-mass frame to the laboratory frame. In simple cases, the scattering angles in these two frames are monotonically related so that it is straightforward to assign a nature to a \( \Theta_{LAB} \) value, i.e., forward, sideways or backward of the scattering event. In our studies, where scattering involves an atom and a molecule, the term forward/backward refers in all cases to the trajectory of the atomic reactant.

The differential cross-section \( d\sigma/d\Omega \) for collisions depends on the angle of attack \( \gamma \), the angle between the relative velocity and the molecular axis, and one can expand the differential cross-section as a series of Legendre polynomials

\[
d\sigma(\gamma)/d\Omega = \sum_{l=0}^{\infty} d\sigma_{l}(\mathbf{d})P_{l}(\cos \gamma)
\]

The angle of attack equals either the angle \( \upsilon \) between the dipole and the field or \( \pi - \upsilon \), depending on the direction of the orientation field (parallel or antiparallel to the relative velocity vector). The measured signal, which is an average over the distribution of molecular axes (Eq. 1), depends only on the terms \( l = 0 \) and \( l = 1 \) in Eq. 4. Finally, the observed steric effect given by Eq. 3 is obviously a linear function of the anisotropy parameter \( A_0 \).

The K + CH, I \( \rightarrow \) KI + CH, reaction has been investigated by various groups, each of which measured the angular and velocity distributions of the products at various energies (see [11] for references). All data indicated that KI is scattered with a high probability, in the backward direction in the centre-of-mass frame: this is called a "rebound reaction". Kunz [10] rationalized the result using the DIPR (direct interaction with product repulsion) model, whose basic assumptions are: (i) that the KI molecules undergo at the instant of reaction an impulse directed essentially along the CI vector, so that the KI recoil velocity is strongly correlated to this direction; and (ii) that reaction occurs only if K hits the molecule within a cone-of-acceptance centred around the I-end.

Brute-force experiments have been performed at collision energies at relatively high values (0.79 and 1.24 eV) of the collision energy \( E_{\infty} \) [4]. The observed velocity integrated differential steric effect, defined by Eq. 3, is summarised in Fig. 4a.

The measured steric effect for the reaction K + CH, Br \( \rightarrow \) KBr + CH, is also plotted in Fig. 4a. It is also well represented by the DIPR model assuming slightly different values of the adjustable parameters.

The K + ICI \( \rightarrow \) KI + CI reaction is one of the well-studied prototypes.
of a so-called “stripping reaction”. We have, for the first time, oriented and used a Σ molecule to determine the steric properties of reactive scattering [8].

Experiments were carried out at high collision energies ($E_c = 1.61$ and $3.0$ eV) and the angular and velocity distributions of the products indicated strong forward scattering for both KCl and KI. The main product is KCl but, in contrast to earlier studies performed at lower energies, a significant amount of KI is also produced. Another new feature concerns the recoil velocity distribution of KCl; it exhibits a bimodal distribution owing to the presence of two different pathways for product formation. The high-speed KCl product exhibits a marked negative orientation effect, while no significant effect is observed for the slow product.

Fig. 4b shows the velocity integrated steric effect of the high-speed KCl product. $S(\Theta_{\text{kin}})$ stays essentially negative over the angular range of significant product flux, implying that KCl is preferentially formed if the atom approaches the I-end of the molecule. On the other hand, $S(\Theta_{\text{lab}})$ for KI is positive so the formation of KI requires the atom to approach the Cl end. The solid lines in Fig. 4b are calculated on the basis of the DIPIR model, and they essentially provide a quantitative fit to the experimental data. The reason the wrong ends of the molecule are preferred is unclear.

**Pendular State Spectroscopy**

The concept of pendular states is very fruitful in spectroscopy. Obviously, the Stark effect on molecular spectra has been studied for a long time, and one could fear that pendular states would merely represent a rewording of the same ideas. However, this turns out not to be the case and the pendular description can be used to understand prominent features of molecular spectra, especially at high fields.

When the ratio $\omega = D_B / B$ is made very large, many rotational levels are transformed into pendular levels. The P and R branches of a vibrational transition are replaced by a few equally spaced lines, the spacing being the pendulum quantum. This behaviour was first demonstrated by R.E. Miller and coworkers [12] using the Van der Waals molecule (HCN)$_3$, chosen because of its large dipole moment and very small rotational constant (see Table).

A second example is the spectroscopy of pendular states of ICl in its A and X electronic states. It was chosen because the dipole moments $D_A$ and $D_X$ of these two states were found to have opposite signs. Owing to this sign difference, the lowest pendular states are localized in different regions of phase space for the X and A states. Thus, in a strong field the transitions connecting these pendular states become very weak, whereas they would remain intense if the two dipoles had the same sign.

Two experiments were carried out by Friedrich and Herschbach [5] and collaborators [13] to test this behaviour. They found good agreement between observations and predicted spectra for opposite signs of the dipole moments. One notes, however, that their assignment of spectral lines was somewhat ambiguous because calculations did not take into account the hyperfine structures.

The same experiment has been repeated [14], together with a complete calculation that included the hyperfine structure. This structure does not modify the general behaviour of the energy levels, but it is important, especially in the A-state, and depends strongly on the level. The dependence can be useful in labelling lines in a crowded spectrum. Fig. 5 gives part of the experimental spectrum as well as simulated spectra for the two possible relative signs of the dipoles $D_A$ and $D_X$. The $R_{00}$ line (defined in [14]) connects localized pendular states and its intensity is very sensitive to this sign. The results show unambiguously that the dipole moments of the A and X states have the same sign. This conclusion is supported by elementary quantum chemistry arguments and has been demonstrated experimentally elsewhere [15].

**Future Developments**

Trying to describe the future of a field is always difficult. One can make a comparison: the manipulation of the position or velocity of atoms by laser techniques is having a great impact on atomic physics. We have considered here the manipulation of the rotational degree of freedom of molecules by an electric field, which can be generalized to magnetic or laser fields, noting however that they unfortunately only align molecules (although their effects may be stronger). The exciting feature is that quantization has a pronounced effect on molecular rotation (as opposed to a weak effect on atomic position). This quantization, which makes the analysis much more difficult, possibly yields more interesting insight.

**References**